

# **Dynamical impact of mountains on atmospheric flows**

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the modelling group of LMD, A. Robertson (IRI, NY), F. D'Andréa, S. Mailler (Météo France),  
O. de Viron (IPG, Paris), P. Viterbo (ECMWF), F. Vial.

- a)Heuristic linear analysis**
- b)Mesoscale dynamics**
- c)Mesoscale dynamics impact on the planetary scale**
- d)Synoptic and planetary scales dynamics**
- e)Improving the synoptic and planetary scales**
- f)Planetary scales dynamics**
- g)Summary of issues**

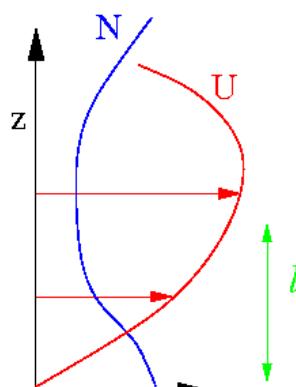
Sorry, this will be the theoretical view of a large-scale modeller!

# Dynamical impact of mountains on atmospheric flows

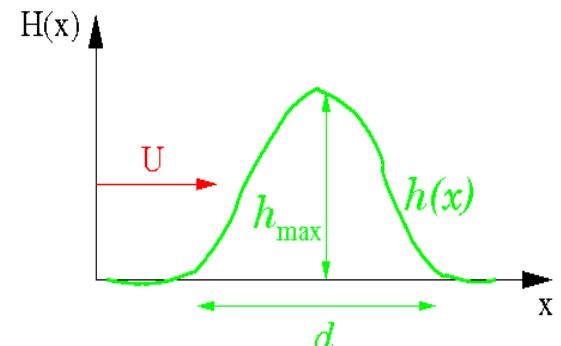
## a) Heuristic linear analysis

## Dimensional analysis:

## Background flow parameters $N, U, l$ , (and $f$ )



# Mountain dimensions $d$ and $h$



## Param. controlling the linear dynamics:

$$Fr^{-1} = \frac{Nd}{U}$$

$$Ro^{-1} = \frac{f d}{U}$$

and low level « trapped waves »:

$$L = \frac{Nl}{U}$$

## Param. controlling the non-linear dynamics:

$$S = \frac{h_{max}}{d}$$

$$H_{ND} = \frac{N h_{max}}{IJ}$$

## Boundary layer dynamics

## Mesoscale dynamics (incl. Gravity waves)

## Synoptic scale and planetary scale dynamics

# *Drag*

$$on \sim \rho C_d U^2 h_{max}$$

## Trapped waves

$$\rho C_a N U h_{max}^2$$

« Vortex Stretching »

$$\rho C_l f U h_{max} d$$

(almost perpendicular to  $U$ )

# *Rossby wave drag*

# *Earth*

$$Fr^{-1}=1$$

$$Ro^{-1} = 1$$

d

# Dynamical impact of mountains on atmospheric flows

## b) mesoscale dynamics ( $f < kU < N$ )

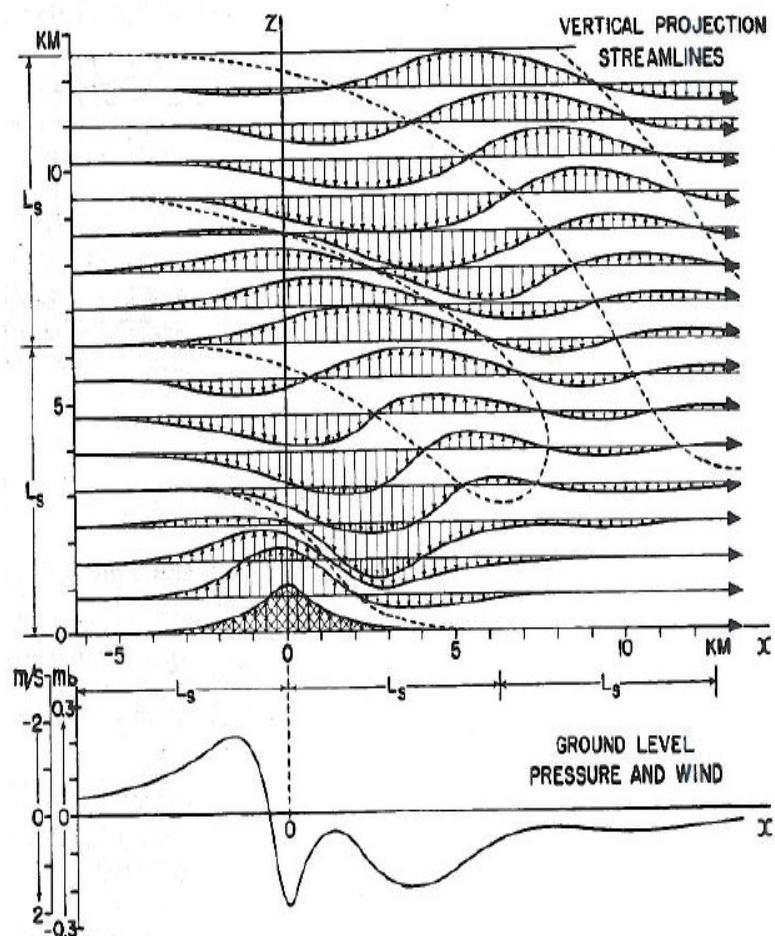
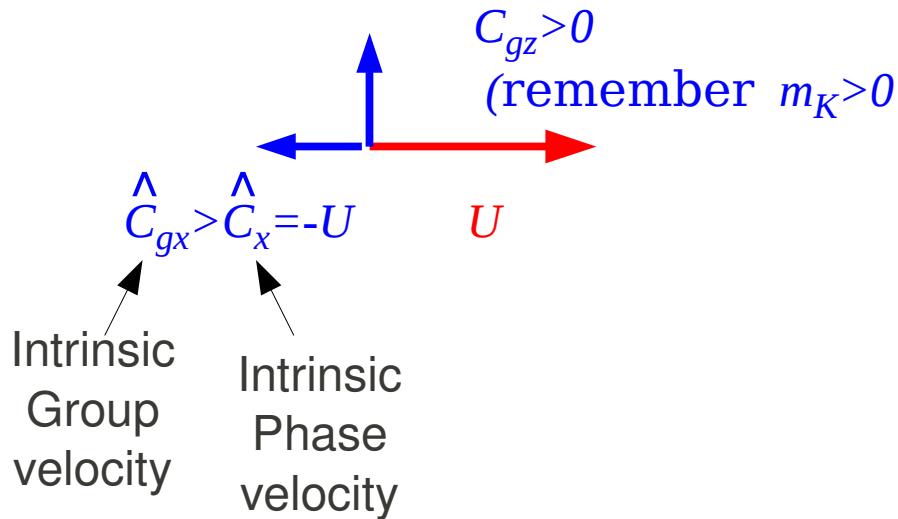
The 2D linear analysis of Queney (1947), mountain drag:  $Dr = \frac{1}{2X} \int_{-X}^X p \frac{dh}{dx}$

$$U=10\text{ m/s}, N=0.01 \text{ s}^{-1}, f=10^{-4} \text{ s}^{-1}$$

$$h(x) = \frac{h_{max}}{1 + \frac{x^2}{d^2}}$$

Case (b):

$d=1\text{ km}$ , non-hydrostatic, non-rotating



# Dynamical impact of mountains on atmospheric flows

## b) mesoscale dynamics ( $f < kU < N$ )

**Linear dynamics and trapped lee-waves** ( $U(z)$  and  $N(z)$  varies)

2D-Boussinesq linear non-rotating theory

$$\frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial z^2} + \left( \frac{N^2}{U^2} - \frac{U_{zz}}{U} \right) w = 0$$

Non  
Hydros-  
tatic

$S(z)$   
Scorer  
parameter

Fourier decomp:  $w(x, z) = \int_{-\infty}^{\infty} \hat{w}(k, z) e^{ikx} dk$

$$\frac{\partial^2 \hat{w}}{\partial z^2} + \left( \frac{N^2}{U^2} - \frac{U_{zz}}{U} - k^2 \right) \hat{w} = 0$$

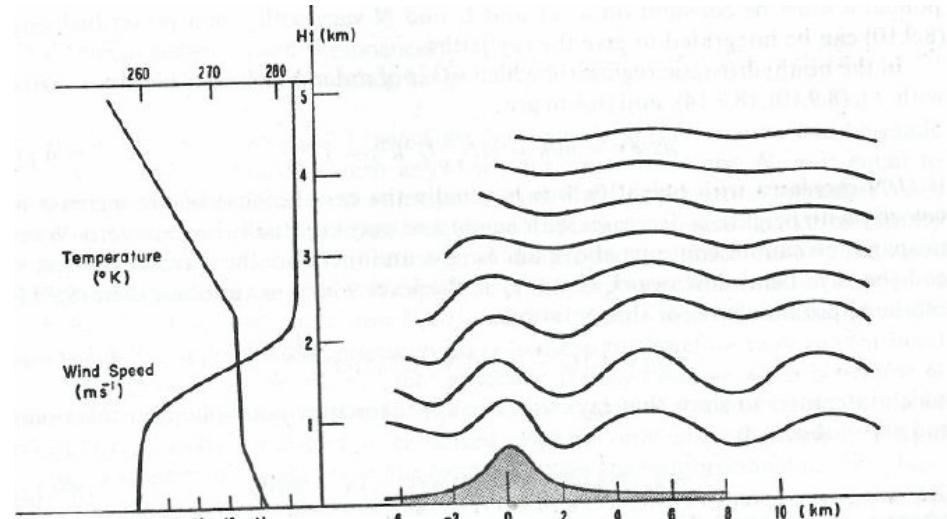
WKB theory:  $m_k^2(z) = S(z) - k^2$

Turning height:  $S(z_c) - k^2 = 0$

WKB theory predicts  $\lim_{z \rightarrow z_c} m_k(z) \rightarrow 0$

Total or partial reflection around  $z_c$

Free modes such that  $w(k, z=0)=0$  can be resonantly excited leading to trapped lee waves



Scorer (1949) + Gossard and Hooke (1975)

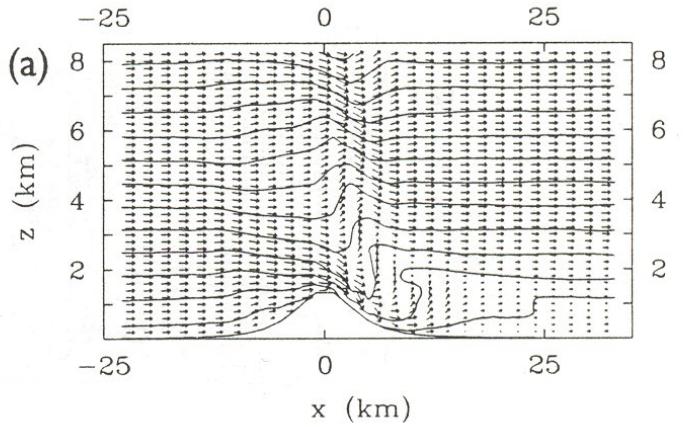
**Issues : Interaction between trapped waves and the PBL**

# Dynamical impact of mountains on atmospheric flows

## b) mesoscale dynamics ( $f < kU < N$ )

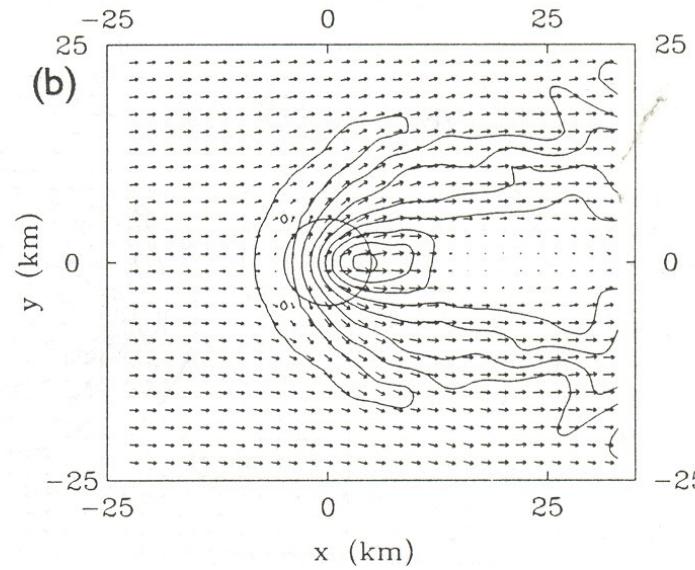
Nonlinear dynamics for Stratified or « slow » Flows :  $Fr^{-1} = \frac{N d}{U} \gg 1$

Single obstacle simulation with  $h \sim 1\text{ km}$ ,  $U = 10\text{ m/s}$ ,  $N = 0.01\text{ s}^{-1}$  :  $H_{ND} = 1$  !  
(Miranda and James 1992)



Note:

Quasi vertical isentropes at low level downstream:  
Wave breaking occurs.



The strong Foehn at the surface downstream

Residual GWs propagating aloft

Apparent slow down near the surface downstream,  
And over a long distance

# Dynamical impact of mountains on atmospheric flows

## c) Mesoscale dynamics impact on the planetary scale

### Subgrid-Scale Orography (SSO) parameterization

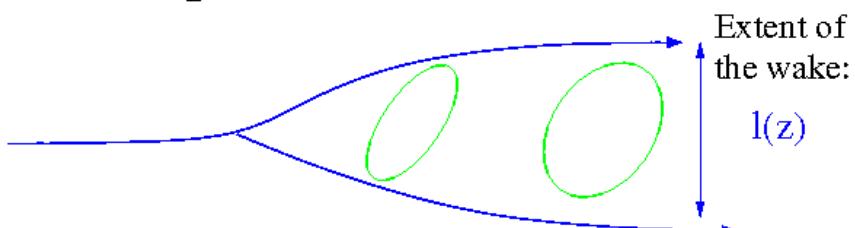
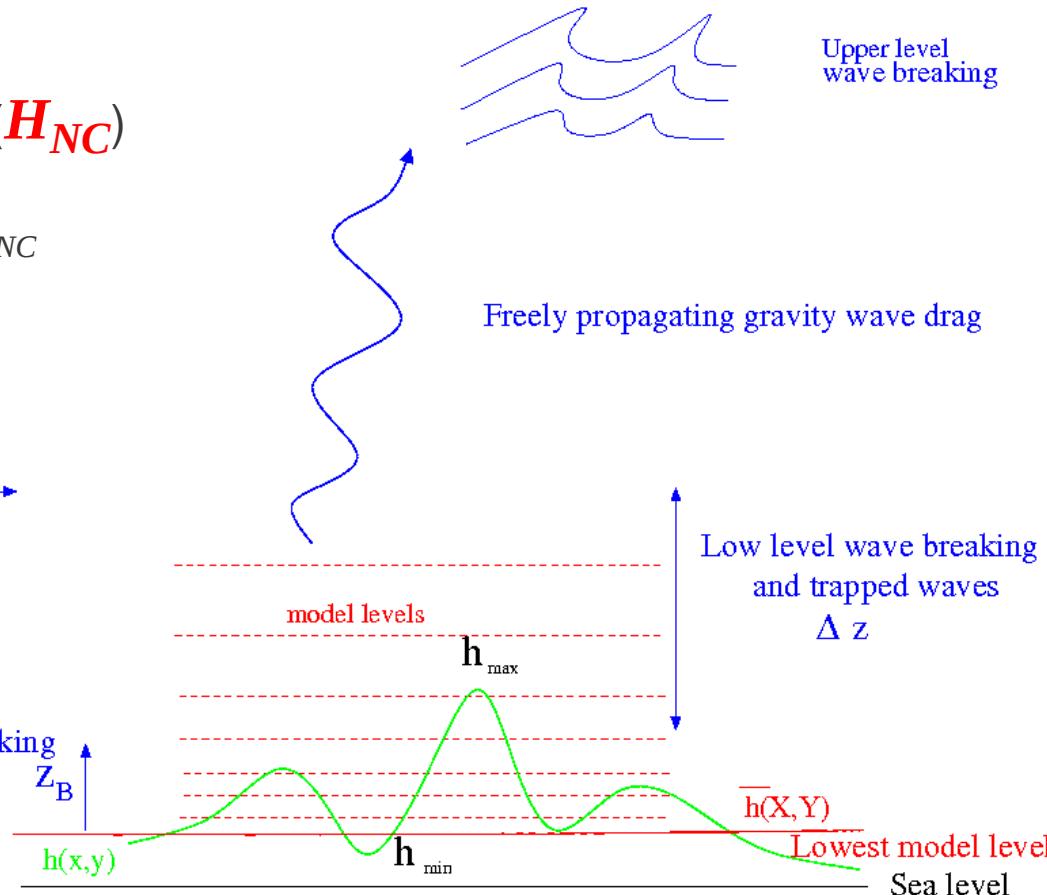
Flow blocking ( $H_{NC}$ )

$$\int_{Z_B}^{h_{max}} \frac{N}{U} dz < H_{NC}$$

$$U(X, Y, z) \\ N(X, Y, z)$$

Flow blocking

$$Z_B$$



Bluff body drag ( $C_d$ ) applied at each model layer that intersects the SSO:

$$\vec{D}_B = -\rho l(z) C_d \frac{\vec{U} \|\vec{U}\|}{2}$$

Breacking based on a total Richardson number criteria ( $Ric$ ):

Gravity wave stress ( $C_g$ )

$$\bar{F}^z = \rho C_g N U (H_{SSO} - Z_B)^2$$

Breaking at low level and Trapped waves are also represented

# Dynamical impact of mountains on atmospheric flows

## c) Mesoscale dynamics impact on the planetary scale

### Subgrid-Scale Orography (SSO) parameterization

Issues about the formulation itself :

Trapped lee waves are parametrized in an ad-hoc way (the theory beneath the Parameterization is essentially hydrostatic)

Concerning mountain waves prediction, the reality is much more stochastic than We could expect from such a steady forcing

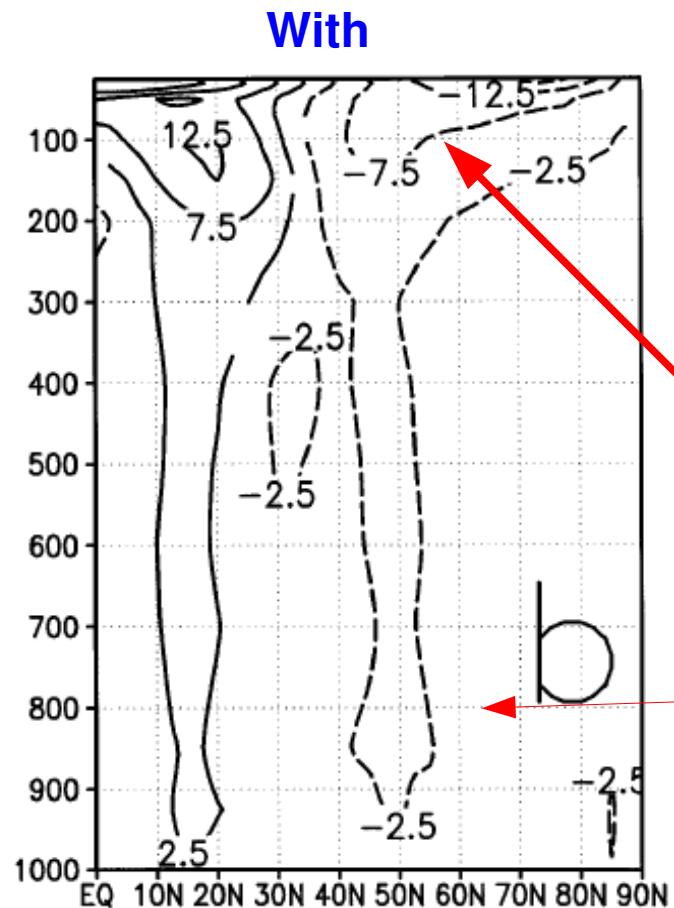
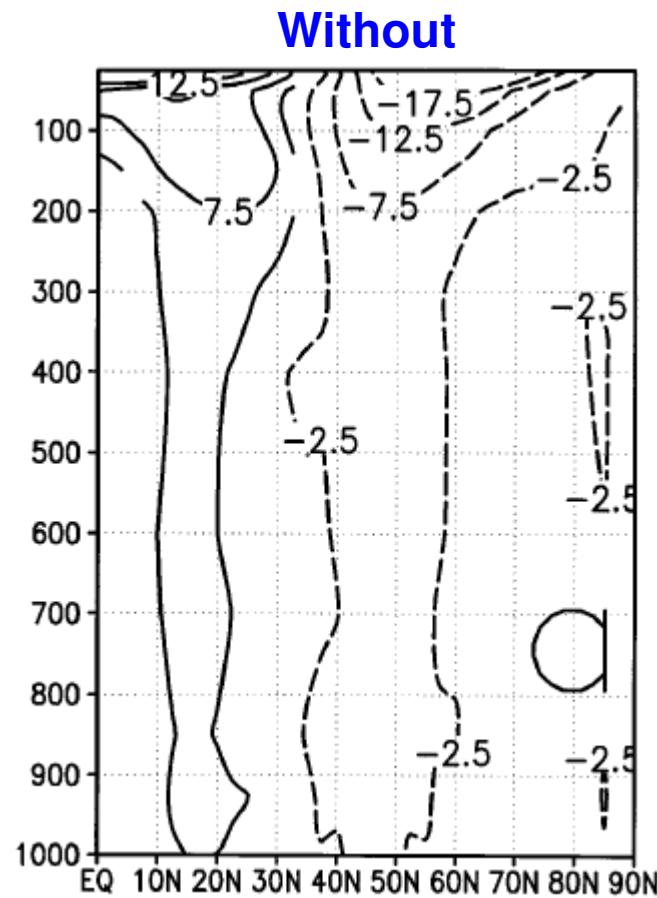
Directional effects have to be re-examined thoroughly

All these can be handled via parameterisations using large ensembles of Monochromatic mountain waves produced stochastically (for a good part of their amplitude)

# Dynamical impact of mountains on atmospheric flows

## c) Mesoscale dynamics impact on the planetary scale

Impact in a GCM's troposphere  
Errors and on the zonal mean zonal wind (Analyse-model)



Now it is more  
the SSO drag  
that does the job:

With the upper level  
gravity waves helping  
close the jet at the  
Tropopause

The low level  
drag reducing the jet  
amplitude in the  
Low and Mid troposphere

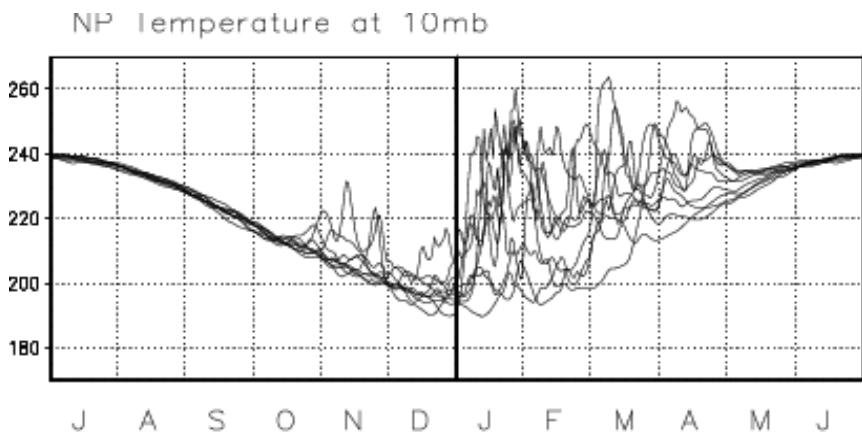
# Dynamical impact of mountains on atmospheric flows

## c) Mesoscale dynamics impact on the planetary scale

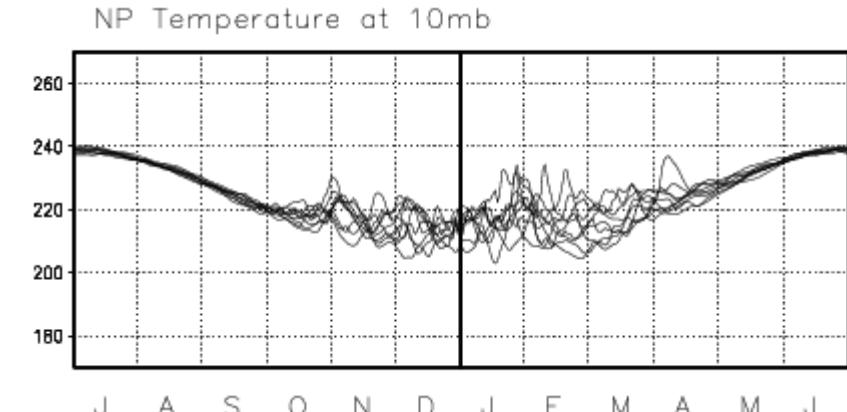
Impact in a GCM's stratosphere

### NH stratospheric warming

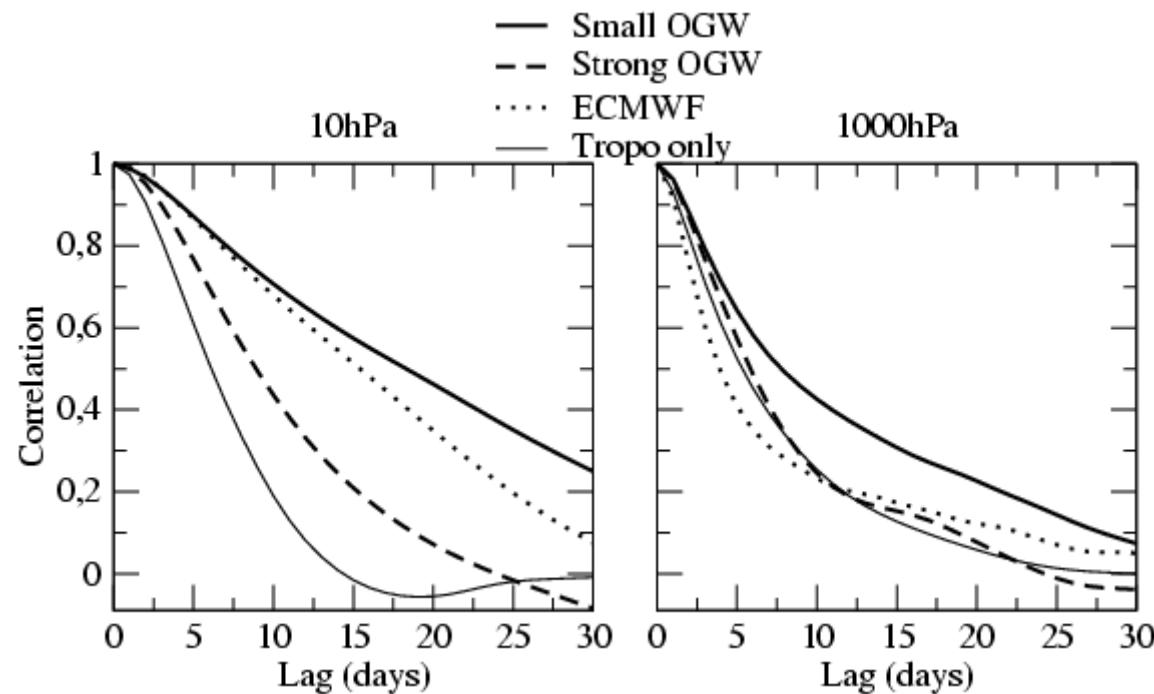
Weak OGWs



Strong OGWs



### Arctic Oscillation persistence

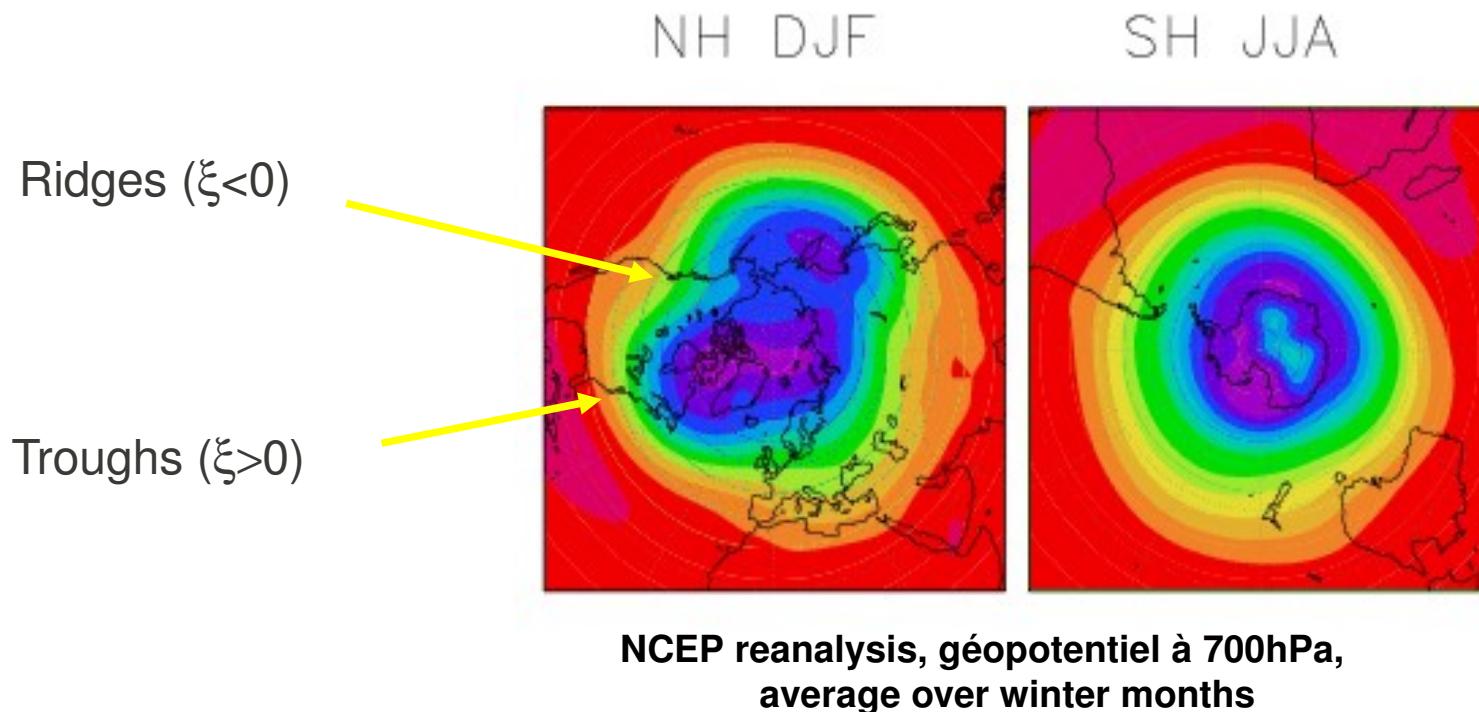


Issues : Effects of GWs in a changing climate.  
Southern hemisphere: case of the  
Andes and of the montaneous Islands  
lost in the southern hemisphere oceans.

# Dynamical impact of mountains on atmospheric flows

## c) Mesoscale dynamics impact on the planetary scale

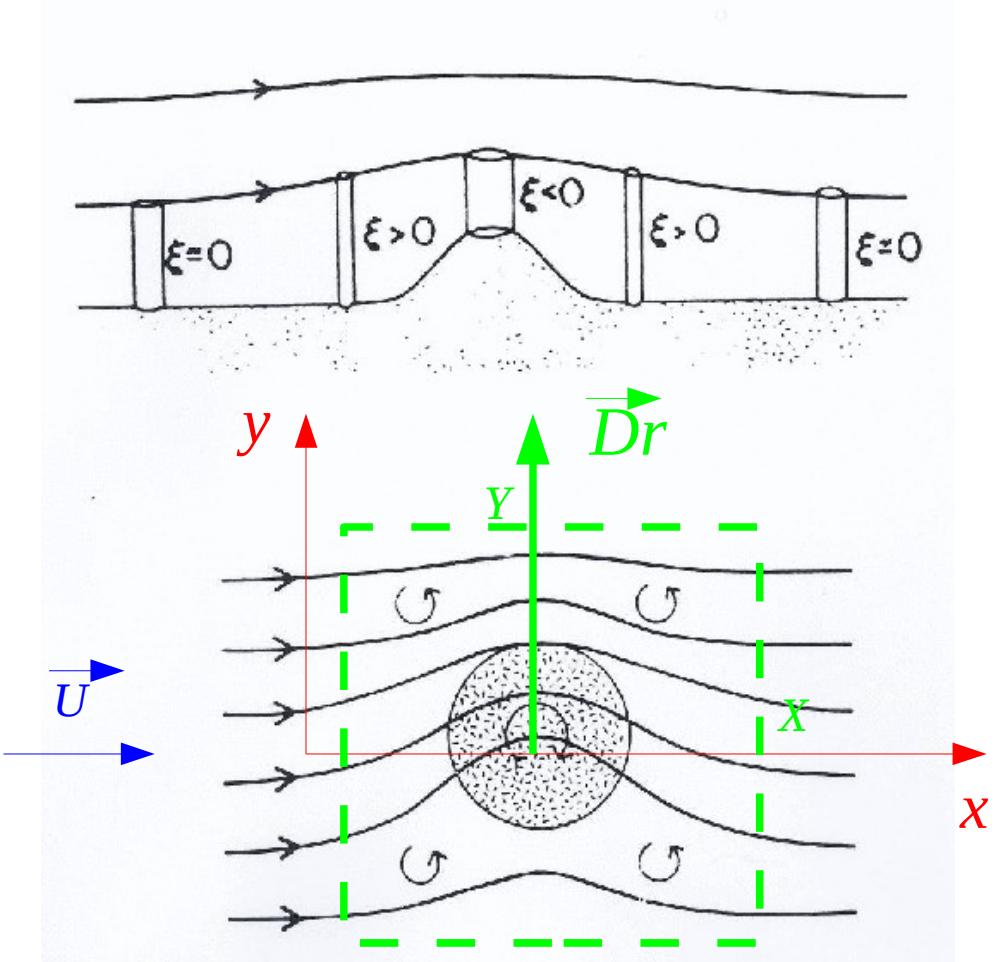
Although the Lott and Miller (1997) SSO drag scheme improve the performances of the ECMWF forecasts (e.g. few days simulations) And the LMDz GCM zonal mean state, it does not improve the structure of the steady planetary waves in the troposphere in climate simulations.



# Dynamical impact of mountains on atmospheric flows

## d) Synoptic and planetary scales dynamics

Basic mechanism is vortex stretching (linear theory):



The force exerted on the mountain is almost perpendicular to the low level incident wind (like a lift force!).

It follows that the mountain felt the background pressure meridional gradient in geostrophic equilibrium with the background wind :

$$P = P_s - f U y$$

$$\vec{Dr} = \frac{1}{4XY} \int_{-Y}^Y \int_{-X}^X + p \vec{\nabla} h dx dy$$

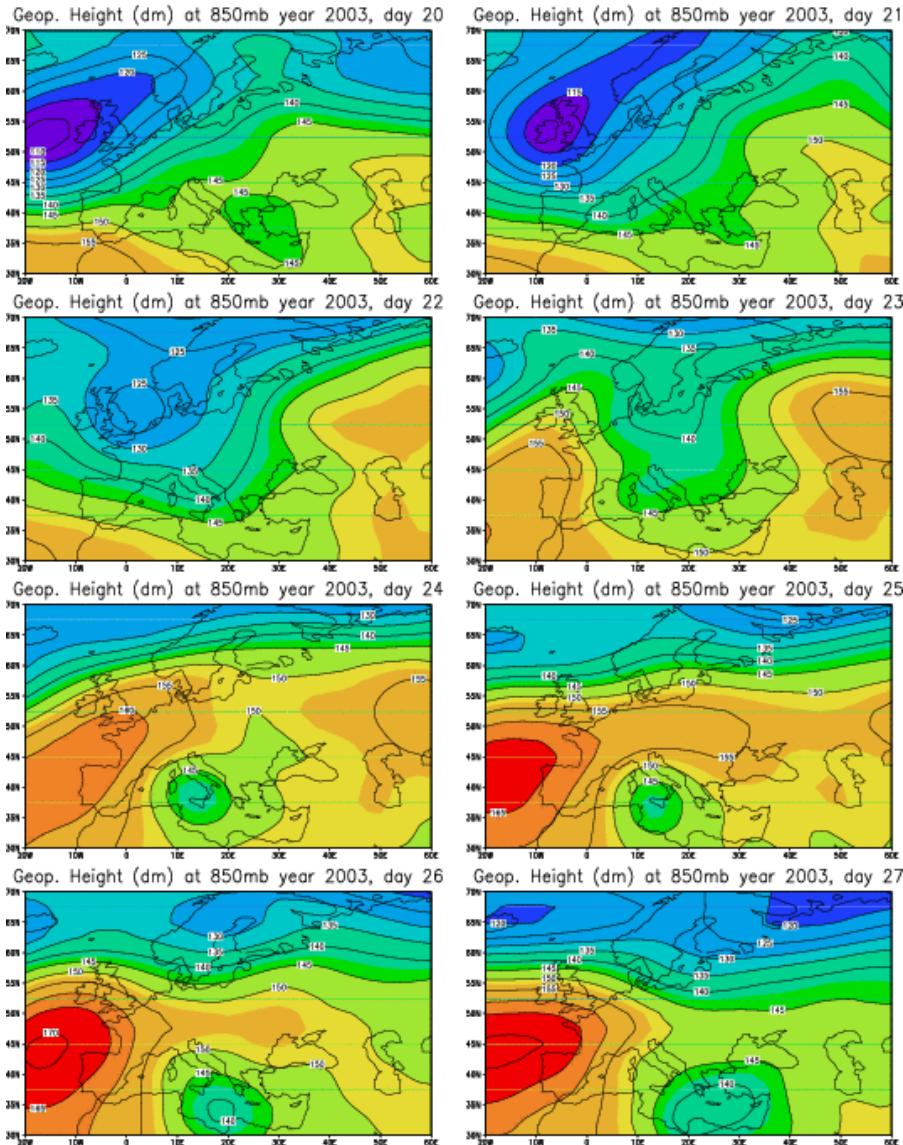
In the linear case:

$$\vec{Dr} = \rho f U \bar{h} \vec{y}$$

# Dynamical impact of mountains on atmospheric flows

## d) Synoptic and planetary scales dynamics

### A case of lee-cyclogenesis (NCEP Data)



This basic mechanism is in part operand during the triggering of mountain lee Cyclogenesis.

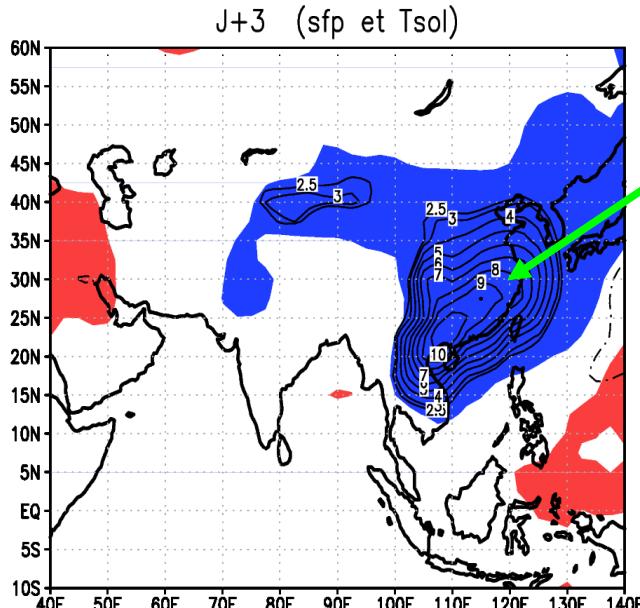
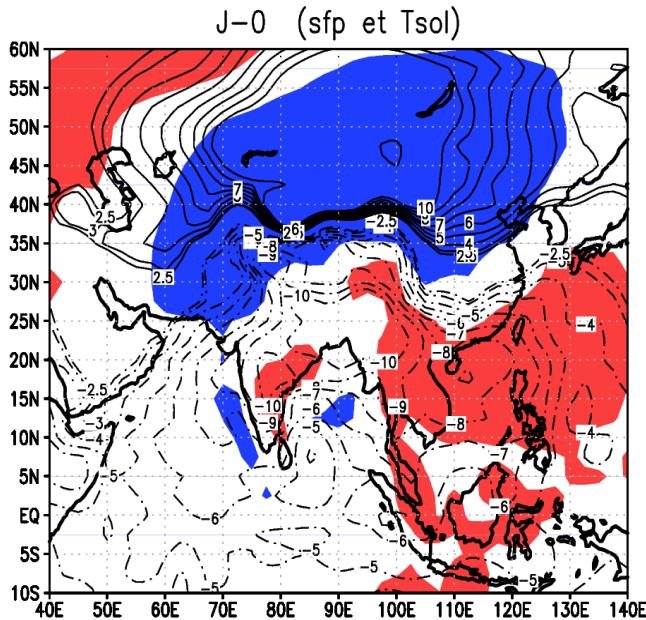
The lift force therefore needs to be well represented in models

# Dynamical impact of mountains on atmospheric flows

## d) Synoptic and planetary scales dynamics

### Relation with Eastern Asia Cold Surges

Composites of surface maps keyed to  $-D_y$  (NCEP Data, 40 cases out of 28 years)



Almost the structure of the cold surges.

Patterns affecting cold surge onset and monsoon precipitations (not shown, but very significant over the South-China sea)

SFP anomaly (contours, Student index), significant surface temperature anomalies  
(blue=cold, red=warm)

Mailler and Lott (2009, 2010)

The peaks of  $-D_y$  are due high pressures and low temperatures over the Tibet to the North of the Himalayas

These structures are few days systematic precursors of the *Cold Surges*, the cold surges producing high negative values in  $D_x$

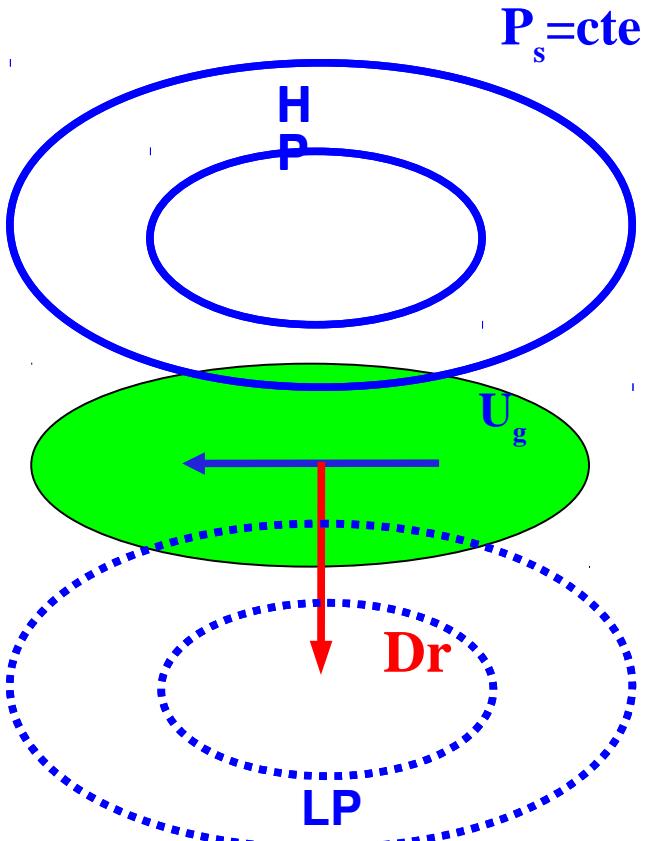
# Dynamical impact of mountains on atmospheric flows

## d) Synoptic and planetary scales dynamics

Basic Mechanism :

How can a lateral force supplement  
the orographic  
forcing ?

View supported by  
A theoretical model



$U_g$ : Geostrophic wind

Dr: Drag

Mountain is in green

$P_s$ : Surface pressure

# Dynamical impact of mountains on atmospheric flows

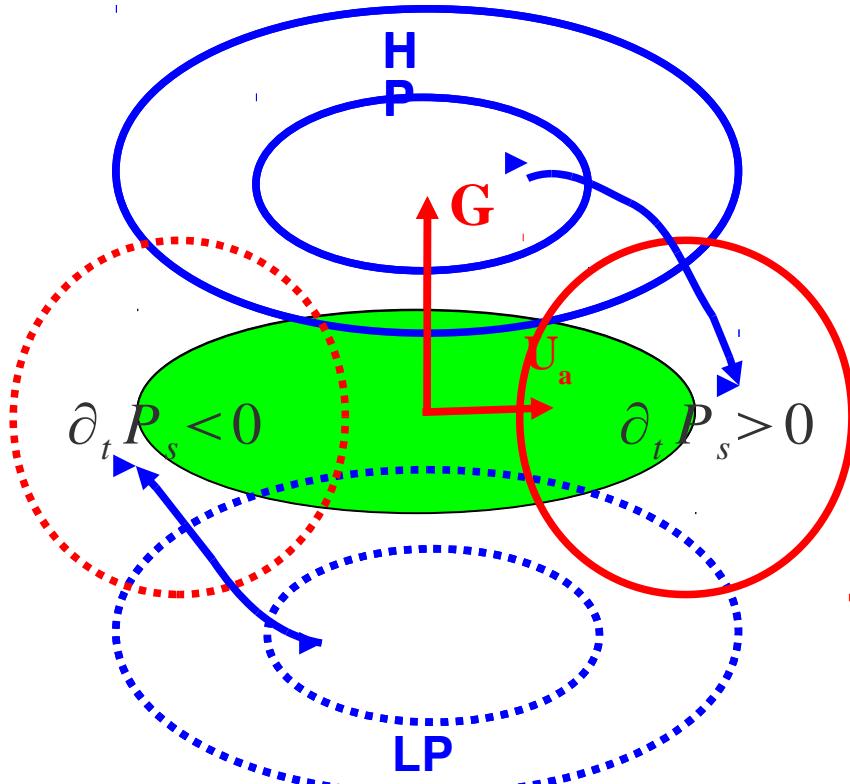
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$$f u_a = G_y$$



**G=-Dr:** the force on the atmosphere is opposite to the drag  
 $U_a$  ageostrophic wind:

Equilibrate  $G$  via Coriolis

Transport mass from left to the right here

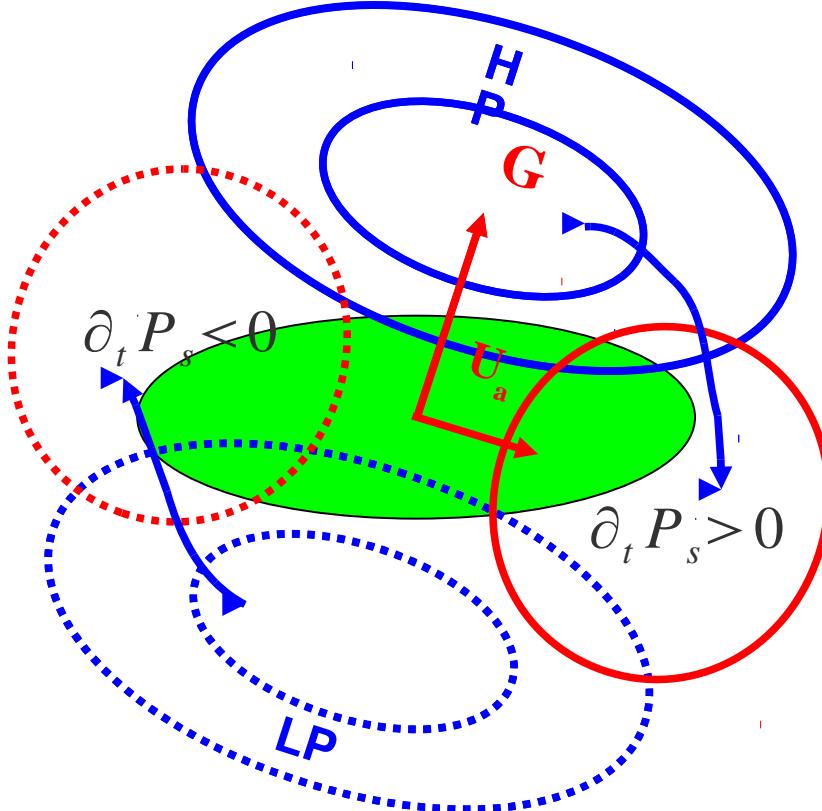
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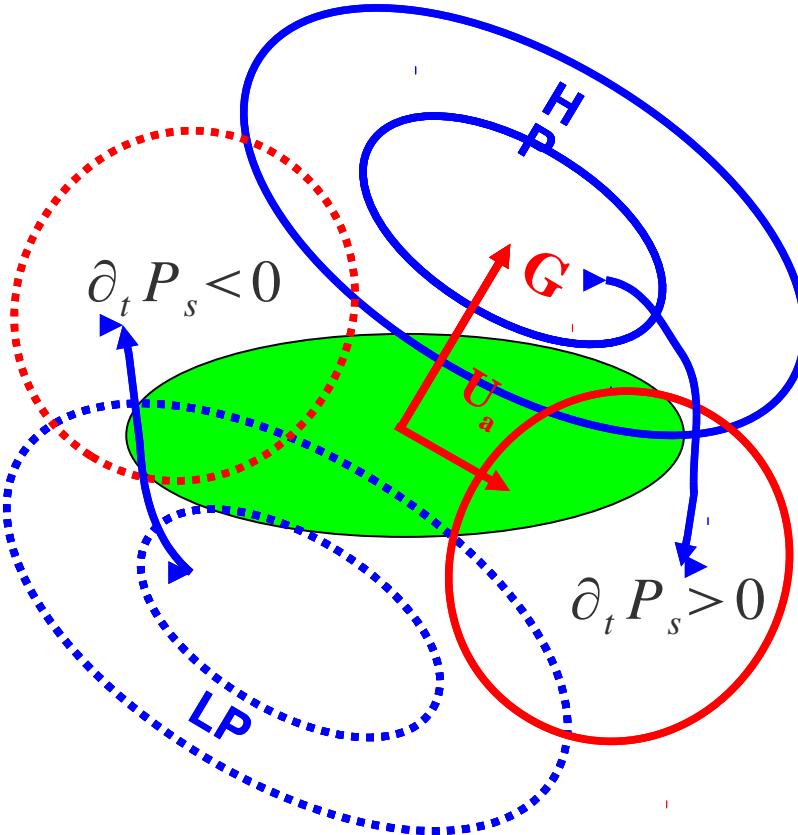
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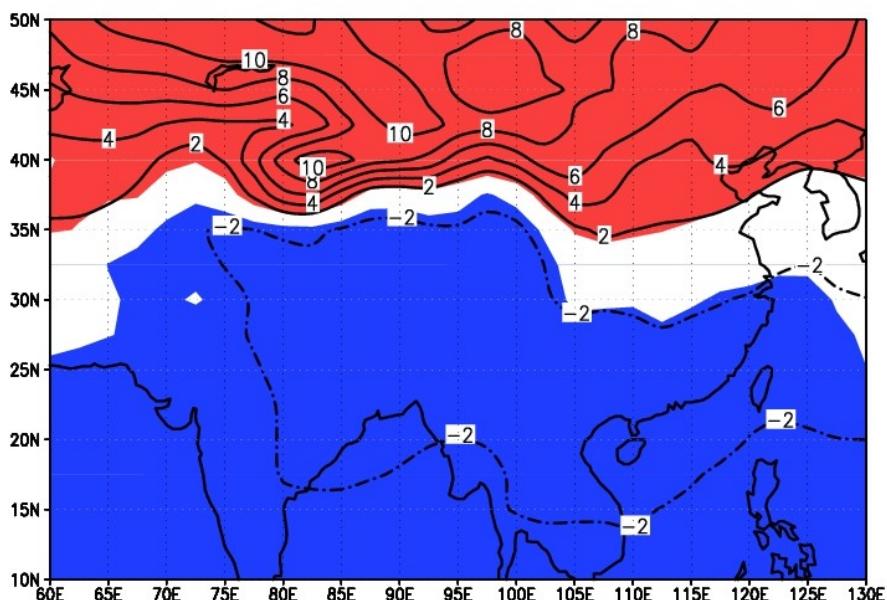
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# Dynamical impact of mountains on atmospheric flows

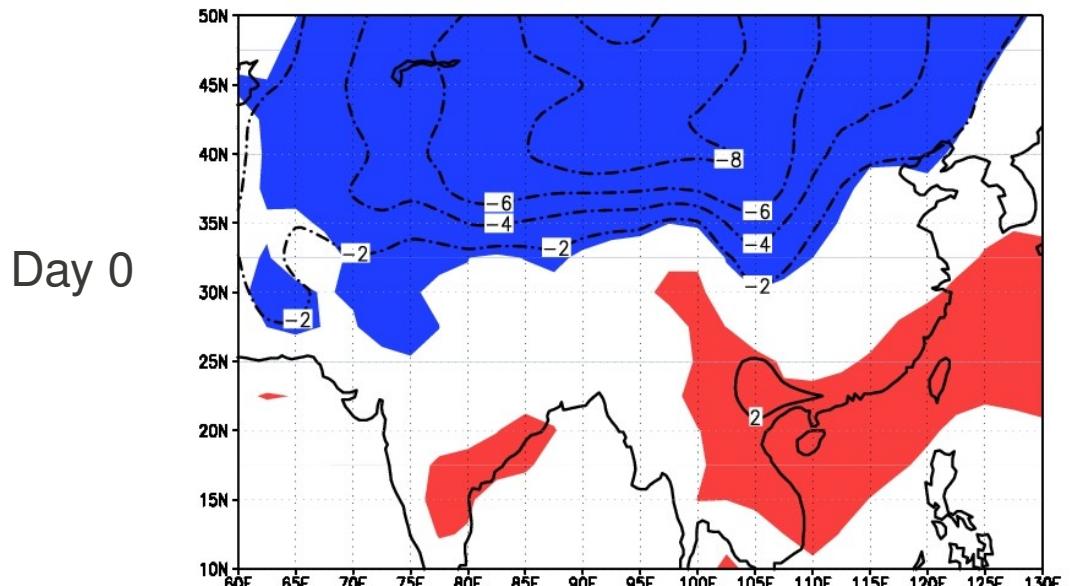
## d) Synoptic and planetary scales dynamics

Composite of anomalies keyed to the anomalous equatorward pressure force  
felt by the Himalayas

Surface Pressure



Surface Temperature



Day 0

Situation corresponding to negative peaks of  $D_{TPy}$ :

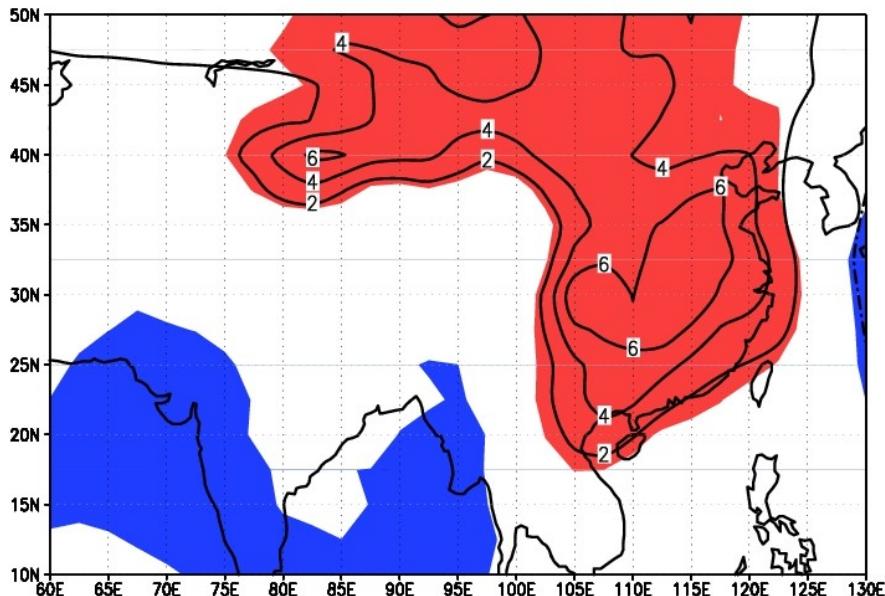
- High pressure and low temperature over Siberia, corresponding to a strengthening of the Siberian High
- Low pressure in the subtropics

# Dynamical impact of mountains on atmospheric flows

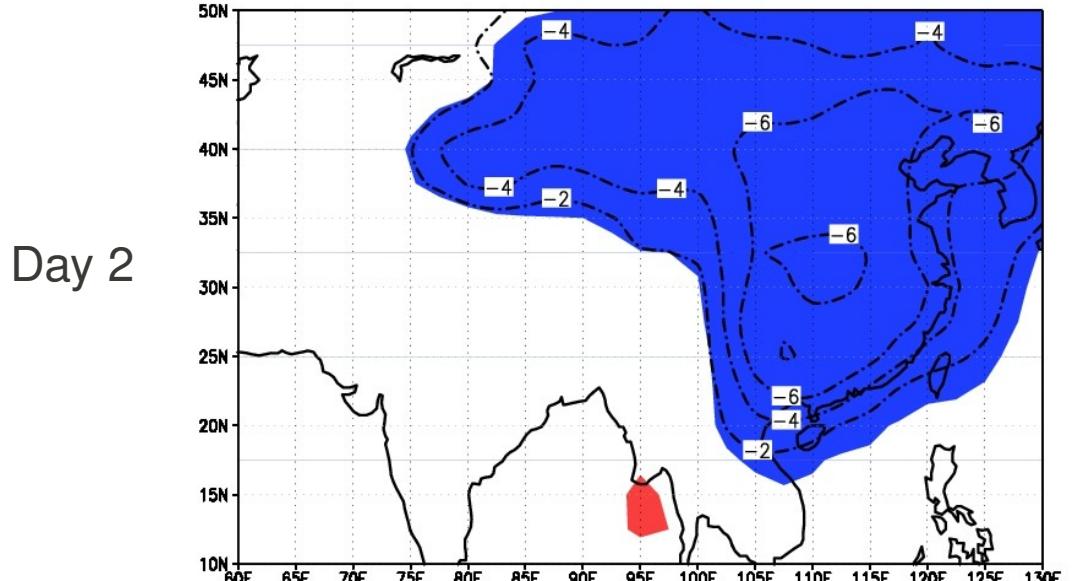
## d) Synoptic and planetary scales dynamics

Composite of anomalies keyed to the anomalous equatorward pressure force  
felt by the Himalayas

Surface Pressure



Surface Temperature



Day 2

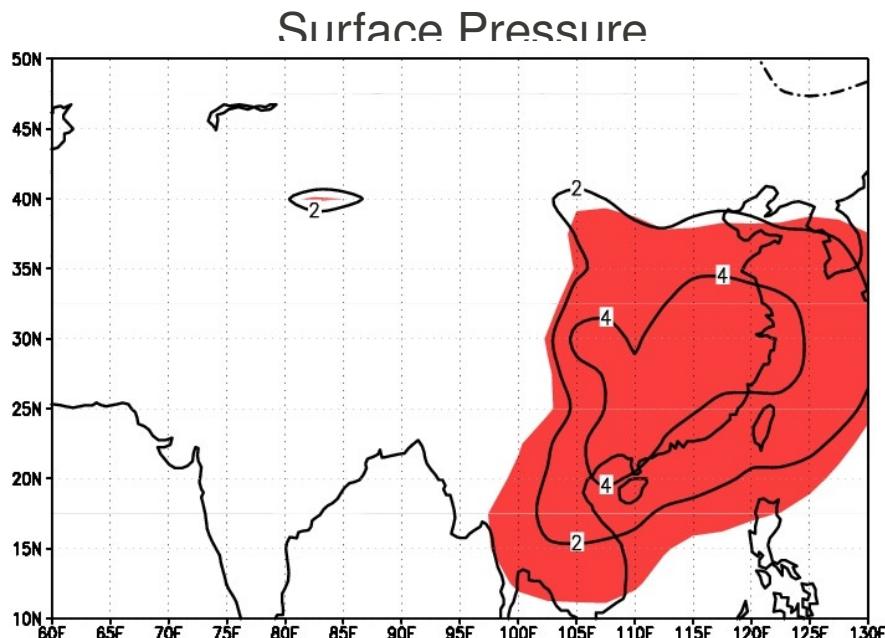
Situation 2 days after :

- Significant high pressure and low temperature in eastern China
- Extends to the subtropics
- Typical of east-asian cold surge

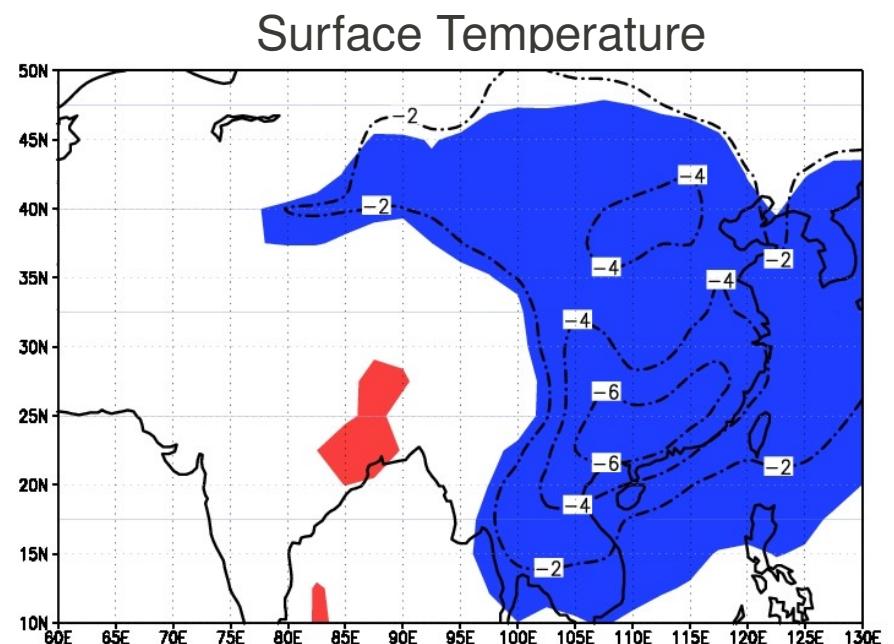
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## d) Synoptic and planetary scales dynamics

Composite of anomalies keyed to the anomalous equatorward pressure force  
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Day 4



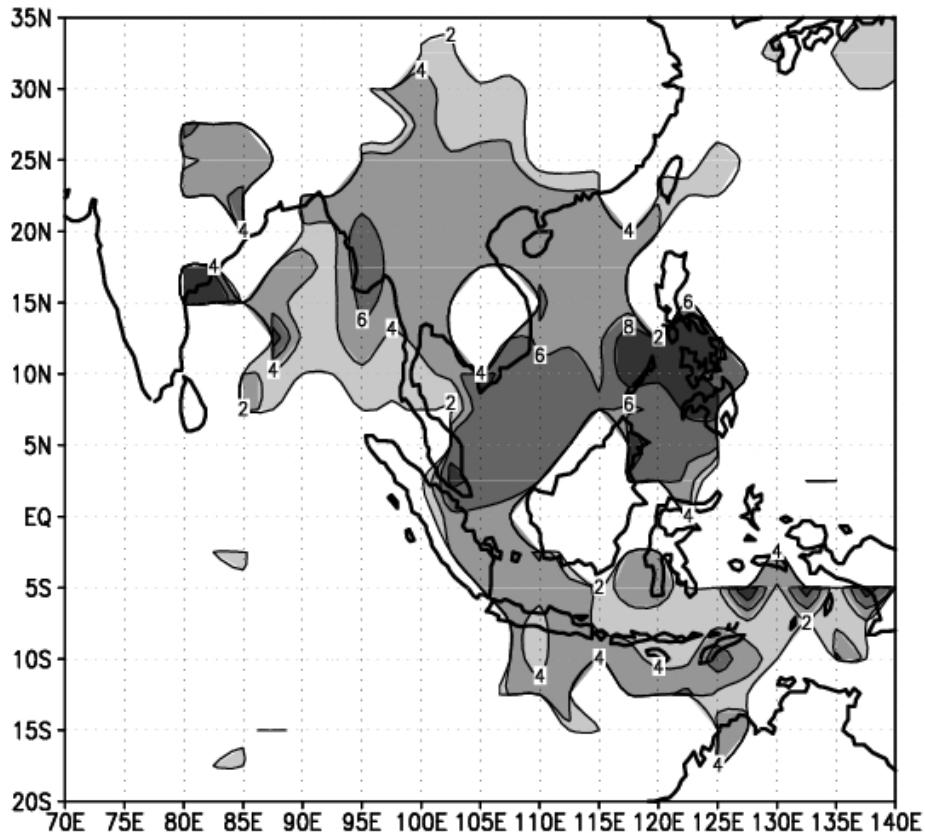
Situation 4 days after :

- Cold surge is mature and strongly affects tropical regions
- Anomalies of surface temperature and surface pressure reach 4 hPa and 6K respectively

# Dynamical impact of mountains on atmospheric flows

## d) Synoptic and planetary scales dynamics

### Impact on precipitations over Southern East Asia



*Zones over which the OLR composite keyed on the intraseasonal  $T_1$  has a significant minimum between D+2 and D+10 (all shaded zones), and lag at which this maximum is reached*

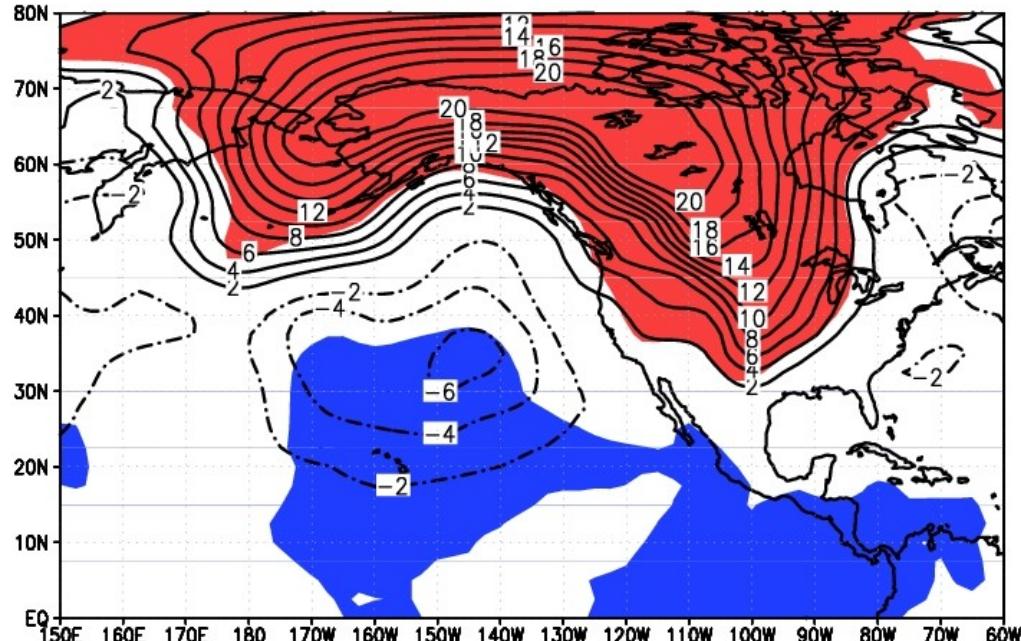
**Issues :** Precipitations near mountain ranges  
In Models.  
Impact of mountain representation  
on precipitations in Models

# Dynamical impact of mountains on atmospheric flows

## d) Synoptic and planetary scales dynamics

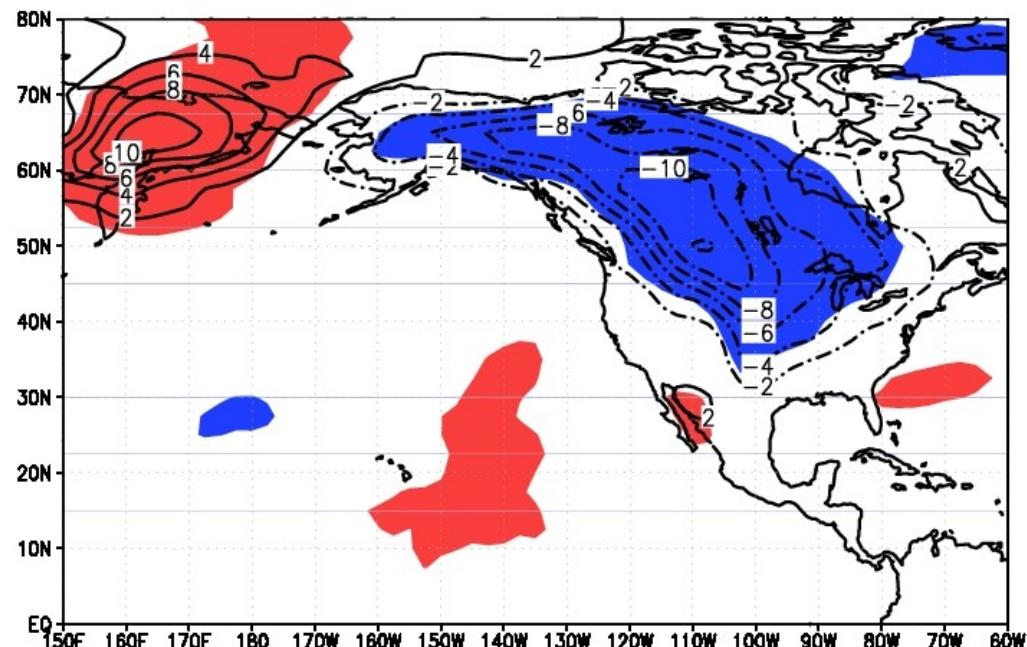
Composite of anomalies keyed to the anomalous equatorward pressure force  
felt by the Rockies

Surface Pressure



Surface Temperature

D0

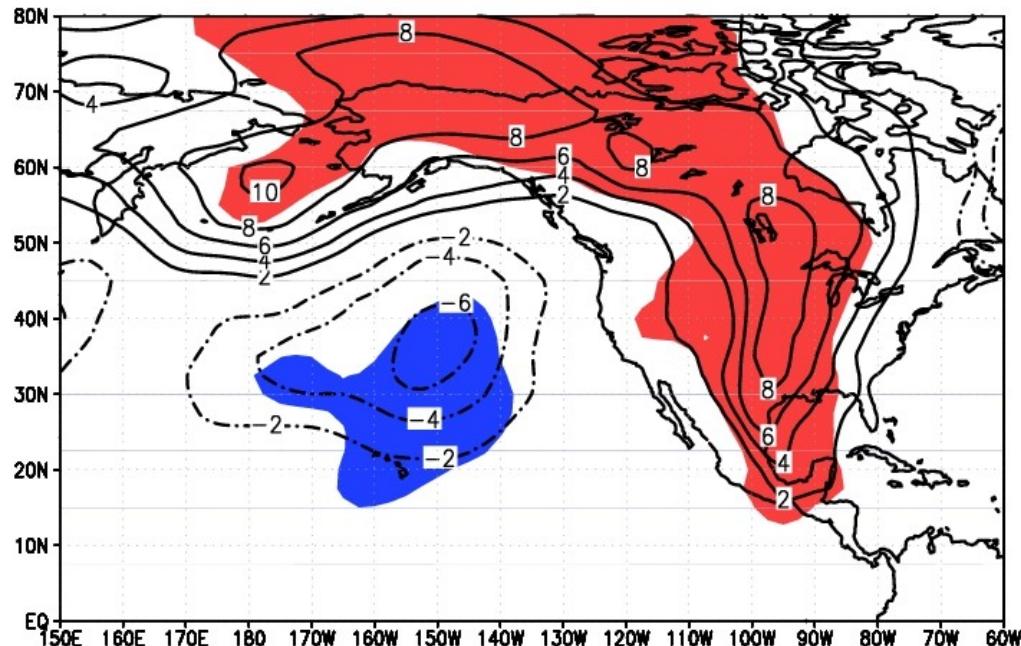


# Dynamical impact of mountains on atmospheric flows

## d) Synoptic and planetary scales dynamics

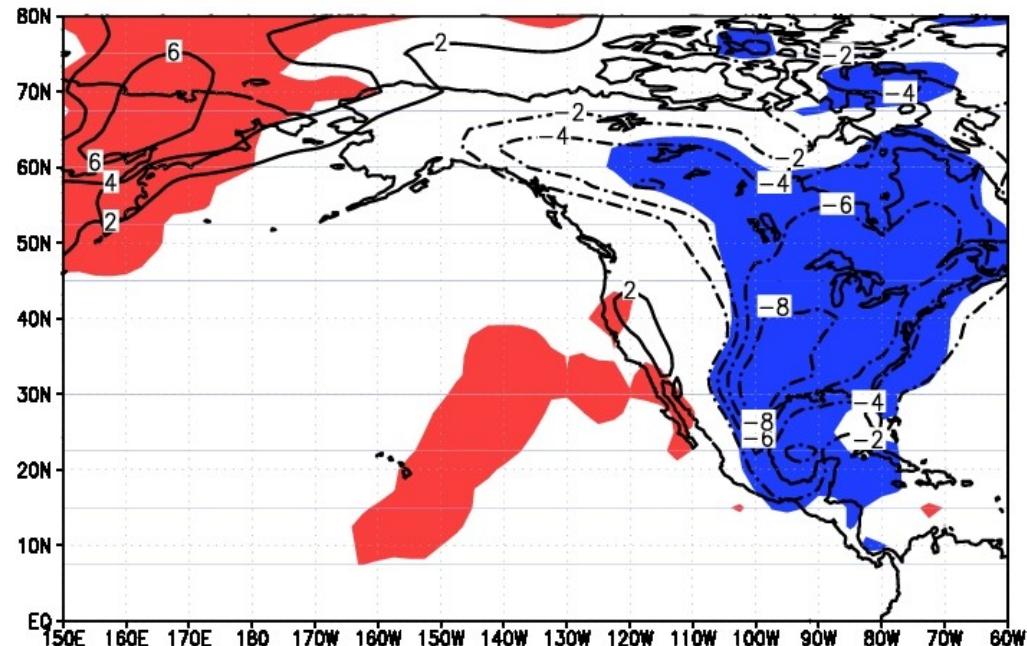
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Surface Pressure



Surface Temperature

D+2

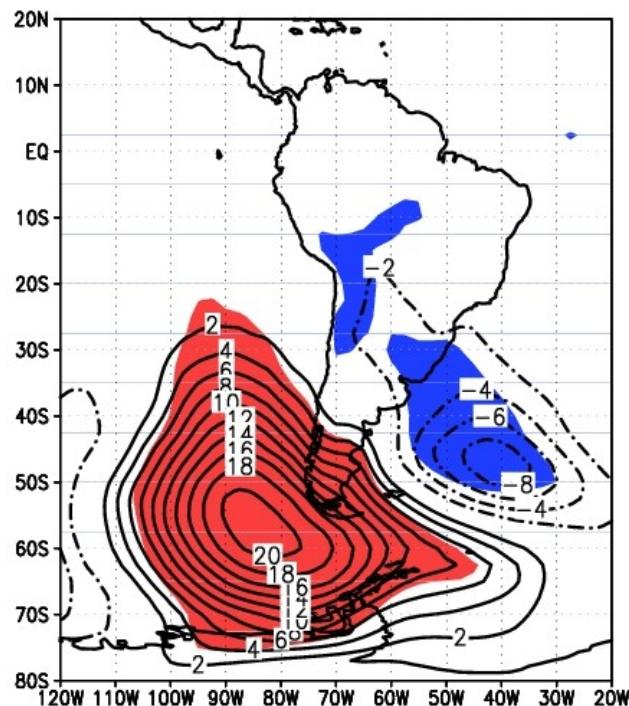


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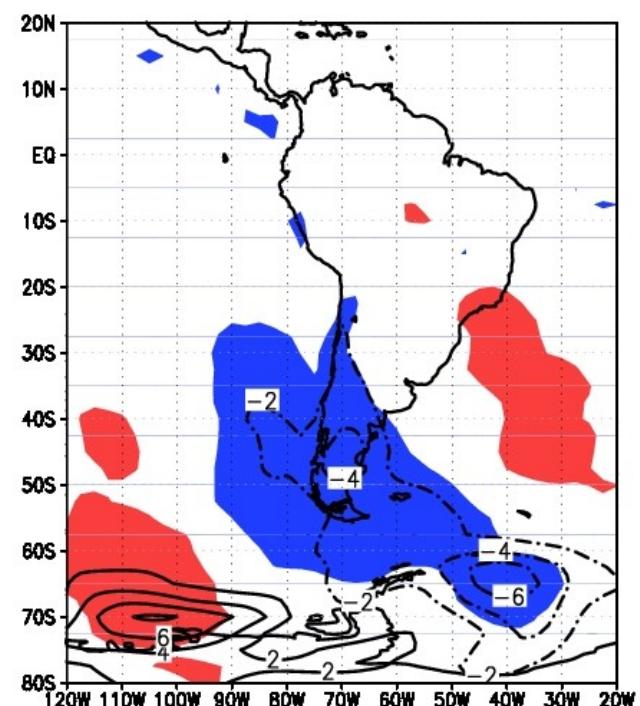
## d) Synoptic and planetary scales dynamics

Composite of anomalies keyed to the anomalous equatorward pressure force  
felt by the Andes

Surface Pressure



Surface Temperature



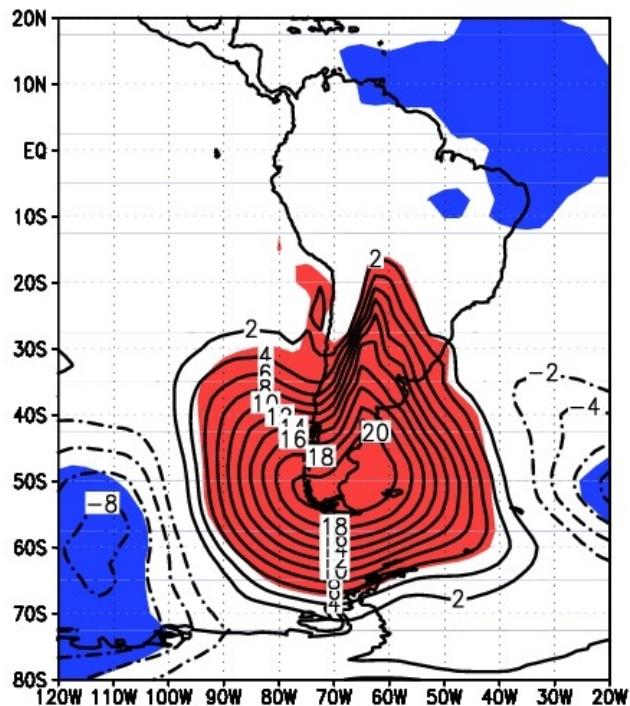
D-2

# Dynamical impact of mountains on atmospheric flows

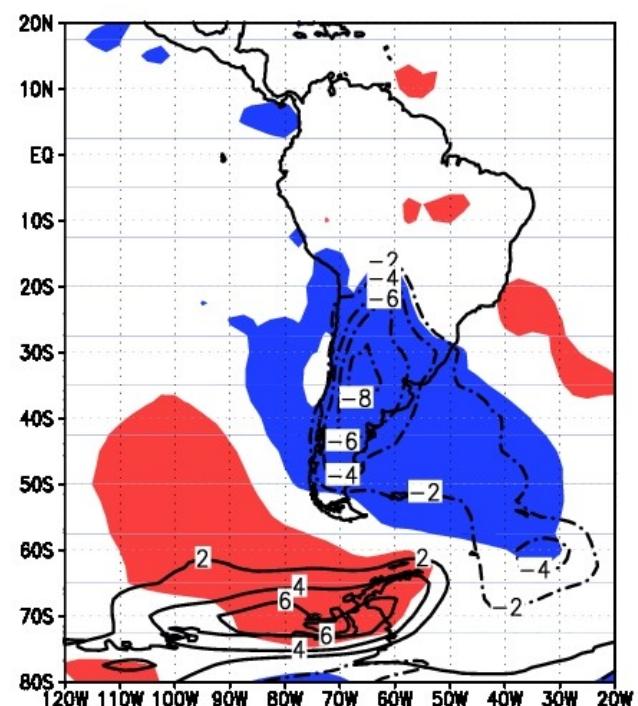
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Surface Temperature



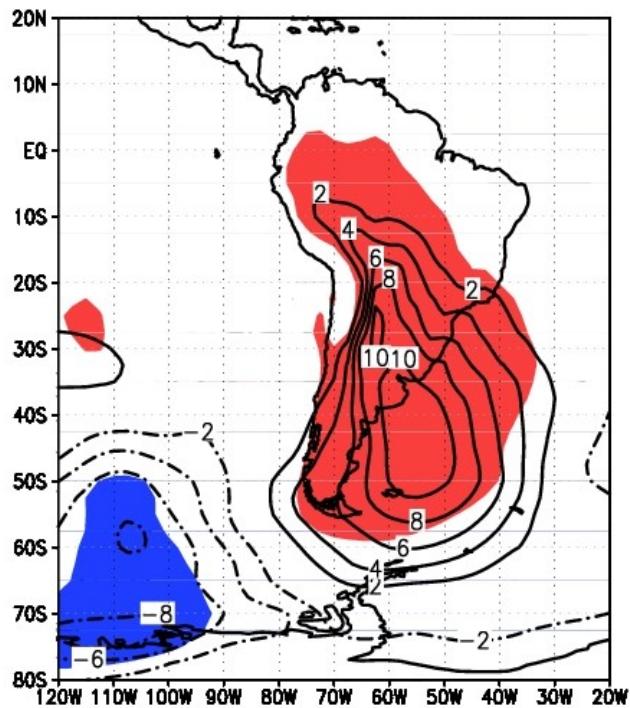
D0

# Dynamical impact of mountains on atmospheric flows

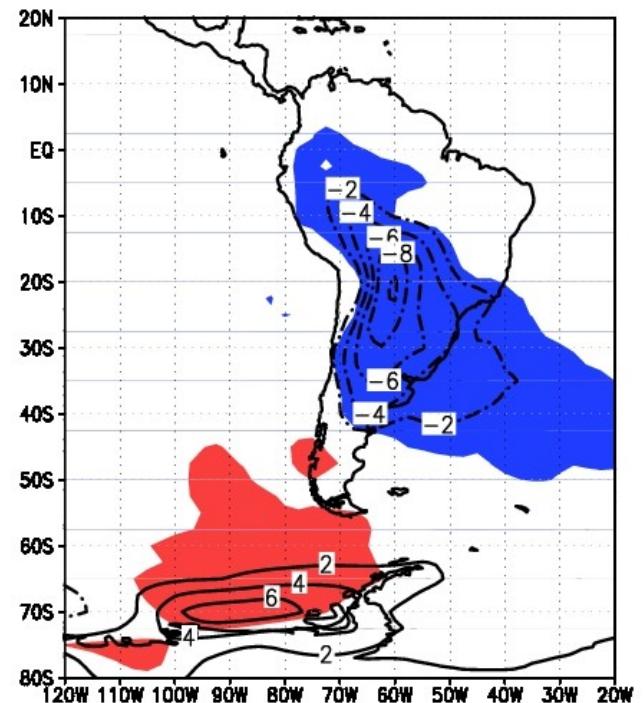
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Surface Temperature



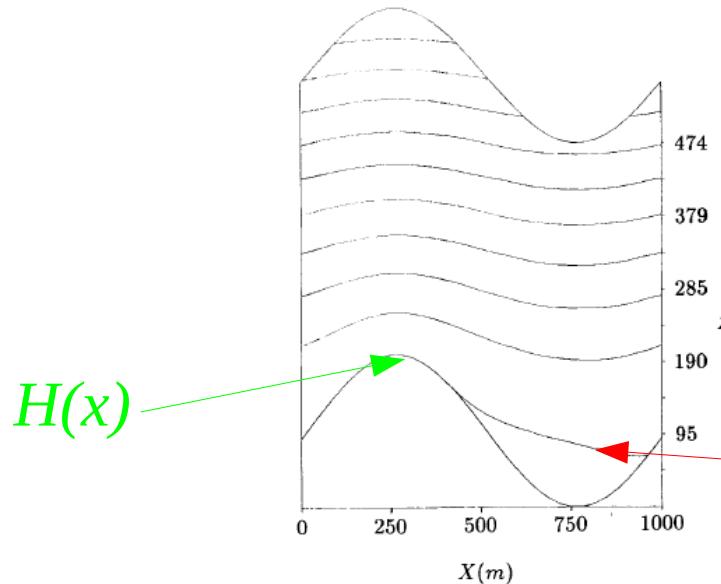
D+2

# Dynamical impact of mountains on atmospheric flows

## e) Improving the synoptic and planetary scales

An argument to enhance vortex stretching over the large scale mountains

Nonlinear effects for mountains of small horizontal scale:  $Fr^{-1} = \frac{N d}{U} \ll 1$



Nonlinear dynamics for  $S = h_{max}/d \sim 0(1)$   
, the slope parameter, it is almost never small!

Streamlines from a 2D Neutral Simulations  
From Wood and Mason (QJ 1993)

$$S = 0.2, Fr^{-1} = 0$$

Note the separation streamline

Figure 1. The model-derived streamlines for flow over the two-dimensional hill with  $h = 200$  m ( $\lambda = 1000$  m and  $Z_0 = 0.1$  m). The vertical axis is linear in height above the upstream surface. The horizontal axis shows distance from the point on the upstream slope at which the hill height is half of its maximum value. A separation streamline is clearly visible.

Hydrodynamic « bluff body » drag:  $Dr \sim \rho C_d \frac{h_{max}}{d} \frac{U|U|}{2}$  (enhanced roughness length in some model)

If the valley is ventilated!! Otherwise the free atmosphere passes over the valleys and hardly see them (this is still an issue)

# Dynamical impact of mountains on atmospheric flows

## e) Improving the synoptic and planetary scales

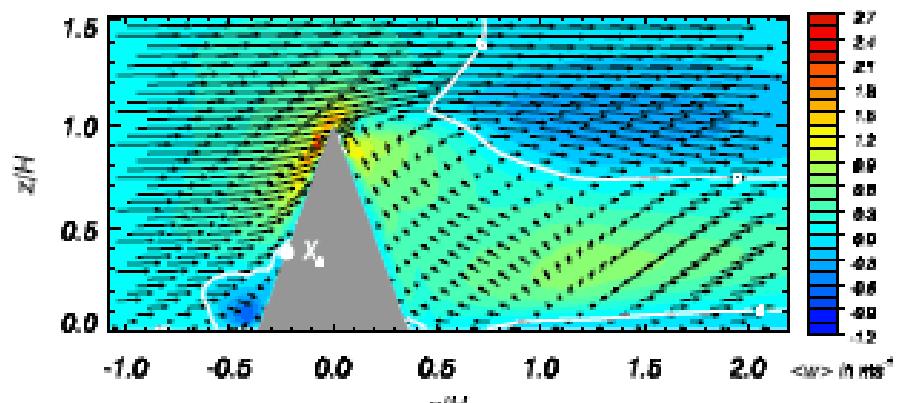
This is the type of dynamics we are talking about

Neutral or Fast Flows :  $Fr^{-1} = \frac{N d}{U} \ll 1$

Nonlinear dynamics for  $S = h_{max}/d \sim 0(1)$



The dynamics at these scales explain the formation of the « banner » clouds aleo of elevated and narrow mountain ridges  
(Reinert and Wirth, BLM 2009)



Large eddy simulation

**Figure 1:** Banner clouds forming leeward of a pyramidal shaped mountain peak or a quasi 2D ridge. (a) Banner cloud at Matterhorn (Switzerland). (b) Banner cloud at Mount Zugspitze (Bavarian Alps). Mean flow from right to left.

# Dynamical impact of mountains on atmospheric flows

## e) Improving the synoptic and planetary scales

A parameterization to improve directly the planetary and synoptic scales:

Higher up the mountains elevation by a fraction of its variance,  
This the concept of envelop orography (Wallace et al. 1983)

An other is to keep a mean orography and to apply the missing forces directly  
in the models levels that intersect the mountain peaks (Lott 1999).

Lift parameter of order 1 ( $C_l$ )

$$\vec{D}_l = -\rho C_l f \left( \frac{h_{max} - z}{h_{max} - h_{mean}} \right) \vec{k} \times \vec{U}$$

When integrated from  $h_{mean}$  to  $h_{max}$  this is the lateral Lift if  $C_l=2$

# Dynamical impact of mountains on atmospheric flows

## e) Improving the synoptic and planetary scales

Illustration of those concepts by parametrizing all the mountains by forces in a GCM (lower model level is everywhere at sea level!). All maps are for geopotential anomalies (e.g. after subtraction of zonal mean values)

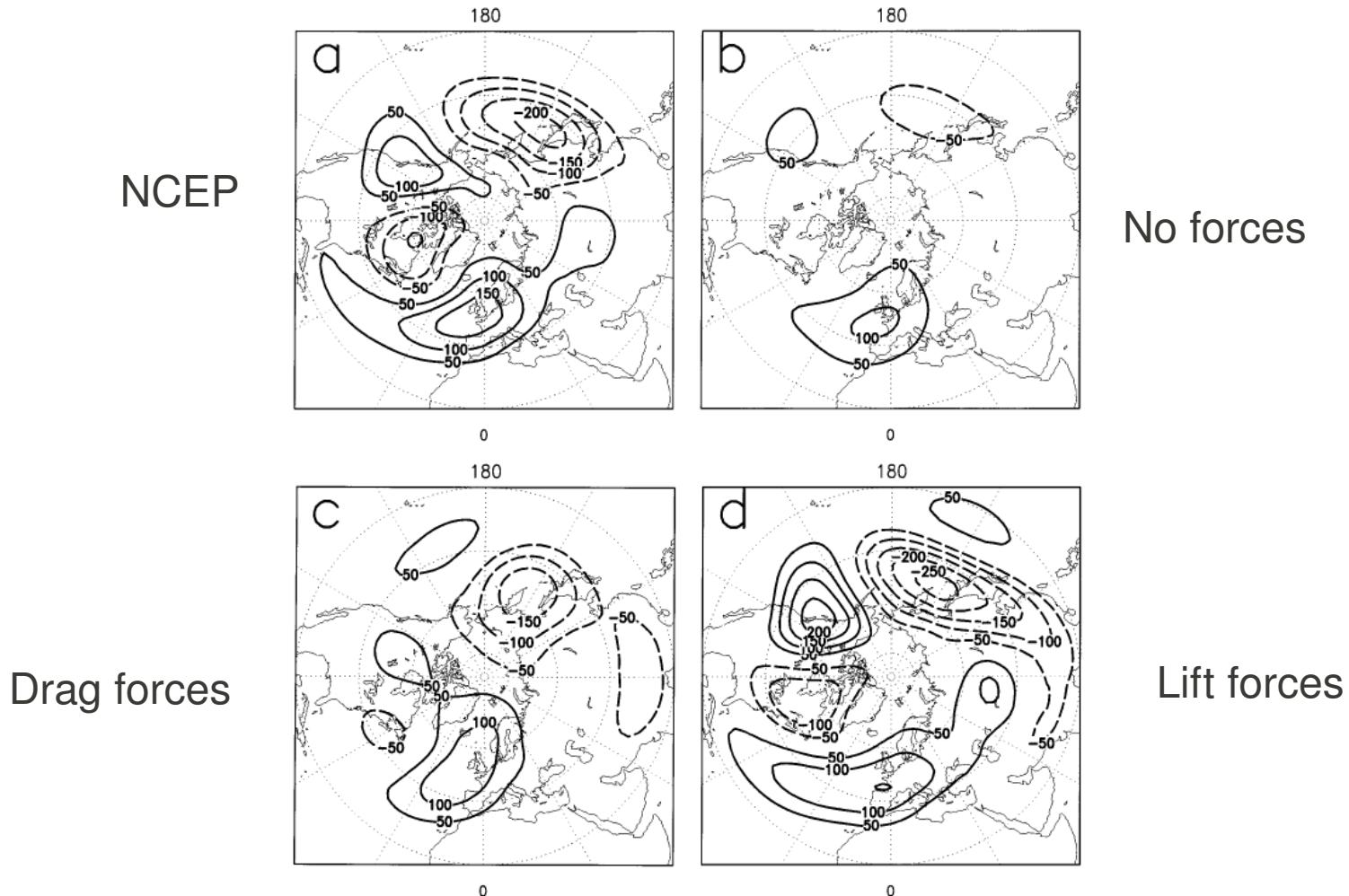


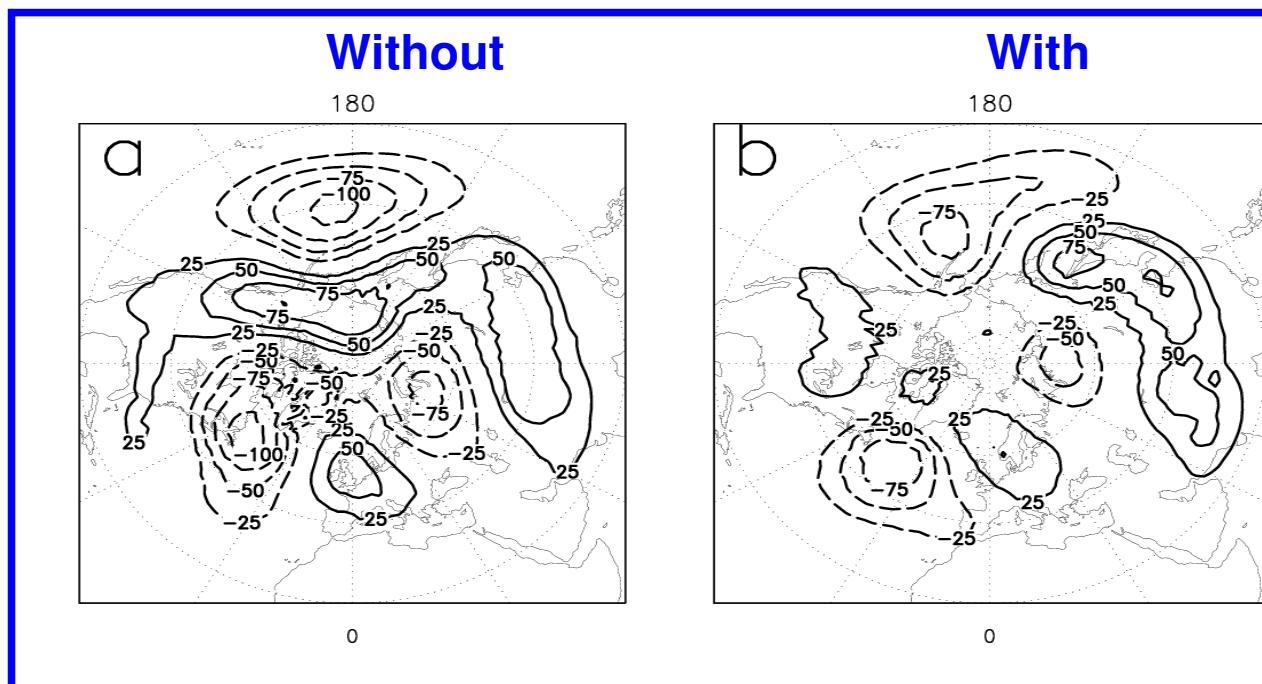
FIG. 3. Anomaly to the zonal mean of the geopotential height at 500 hPa averaged over the winter months (DJF) of the period 1985–90. LMD run with no explicit orography. (a) NMC analysis; (b) LMD no drag, no lift; (c) LMD low drag only; (d) LMD low lift only. Zero line not shown; negative values are dashed.

# Dynamical impact of mountains on atmospheric flows

## e) Improving the synoptic and planetary scales

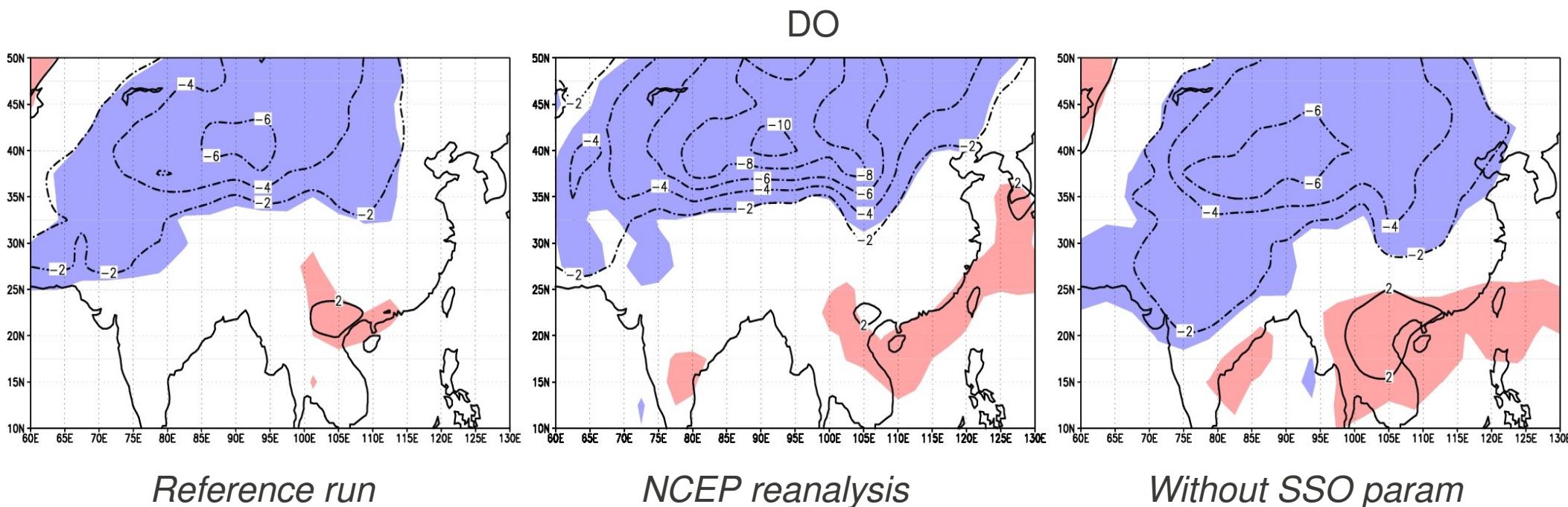
Simulation with mean explicit orography without and with the subgrid scale orographic drag scheme including enhanced lift

Error maps between the Geopotential height at 700hPa,  
NCEP reanalysis minus LMDz  
Winter months out of a 10years long simulation



# Dynamical impact of mountains on atmospheric flows

## e) Improving the synoptic and planetary scales

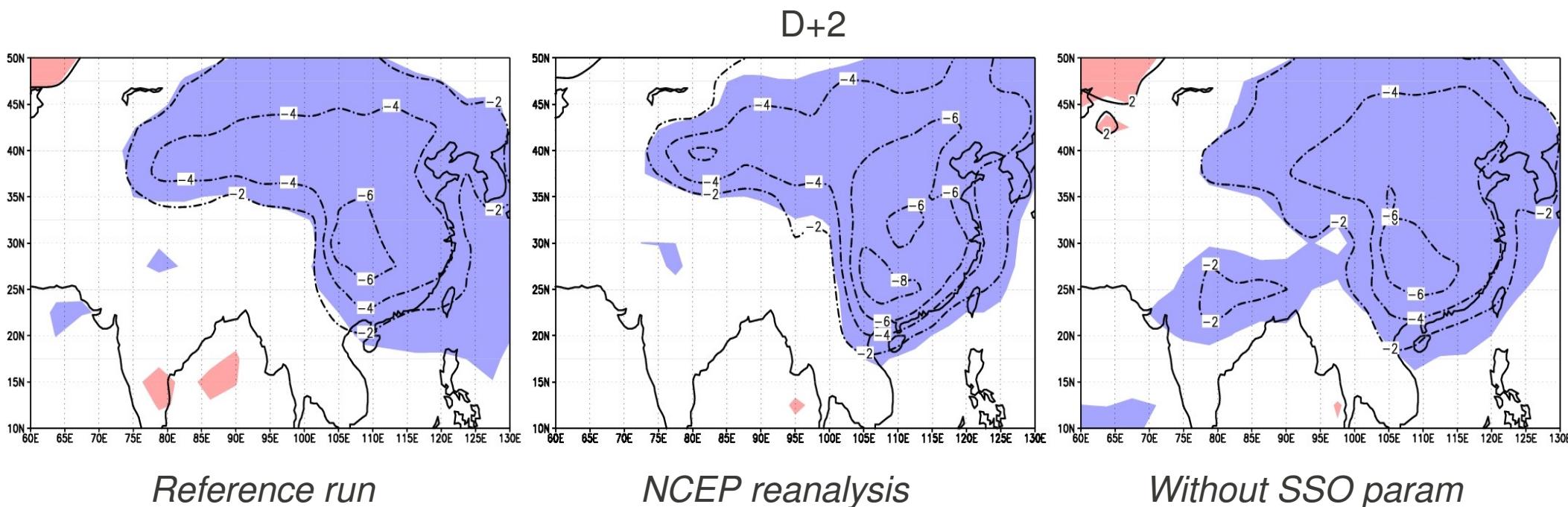


*Composites of surface temperature anomaly keyed on the total Equatorial Torque (LMDz) and on the Equatorial Mountain Torque (NCEP)*

**Issue : does the same improvement occurs for the south-American cold surges?**

# Dynamical impact of mountains on atmospheric flows

## e) Improving the synoptic and planetary scales

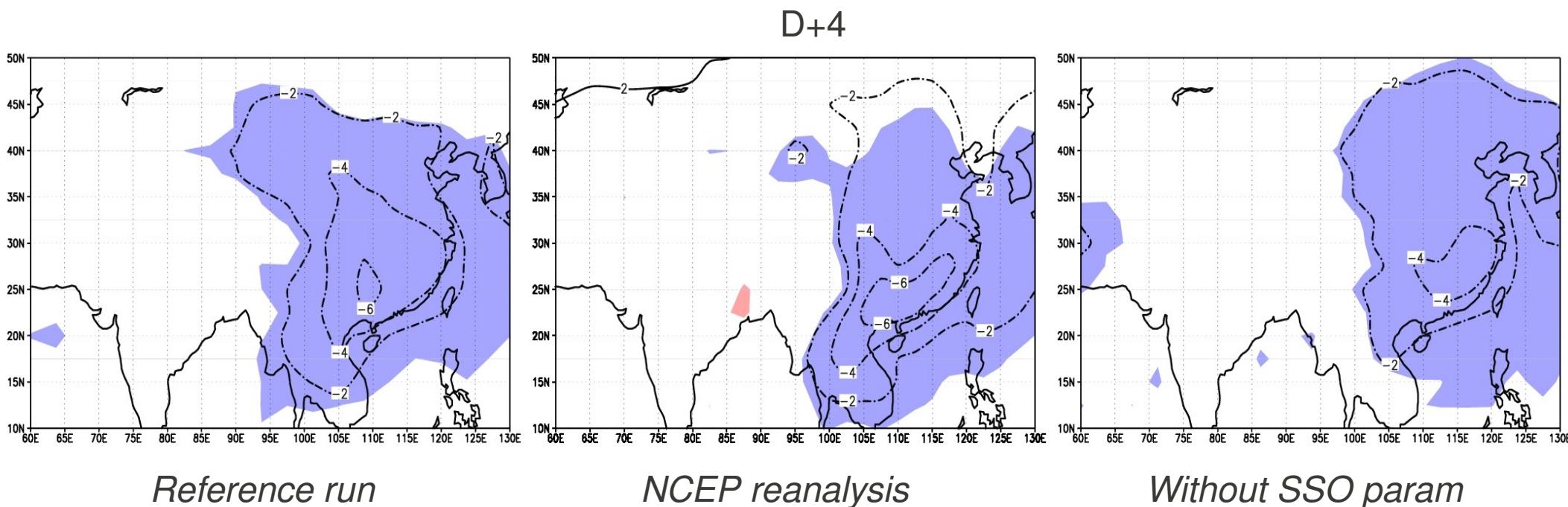


*Composites of surface temperature anomaly keyed on the total Equatorial Torque (LMDz) and on the Equatorial Mountain Torque (NCEP)*

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# Dynamical impact of mountains on atmospheric flows

## e) Improving the synoptic and planetary scales

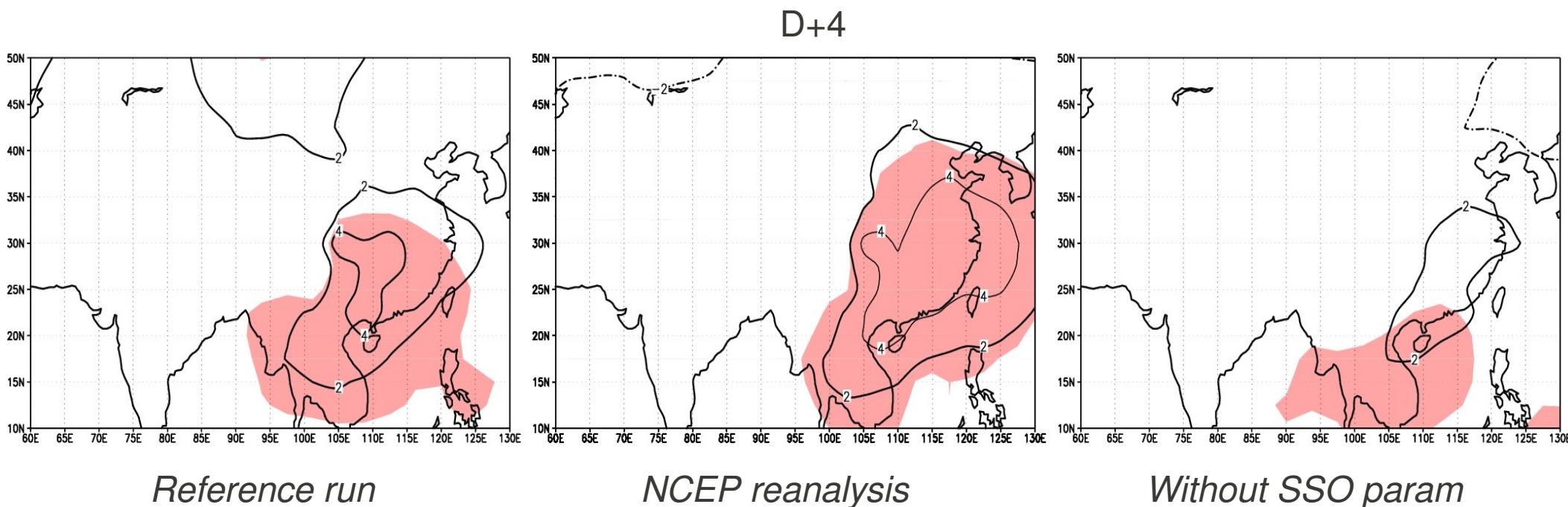


*Composites of surface temperature anomaly keyed on the total Equatorial Torque (LMDz) and on the Equatorial Mountain Torque (NCEP)*

**Issue : does the same improvement occurs for the south-American cold surges?**

# Dynamical impact of mountains on atmospheric flows

## e) Improving the synoptic and planetary scales



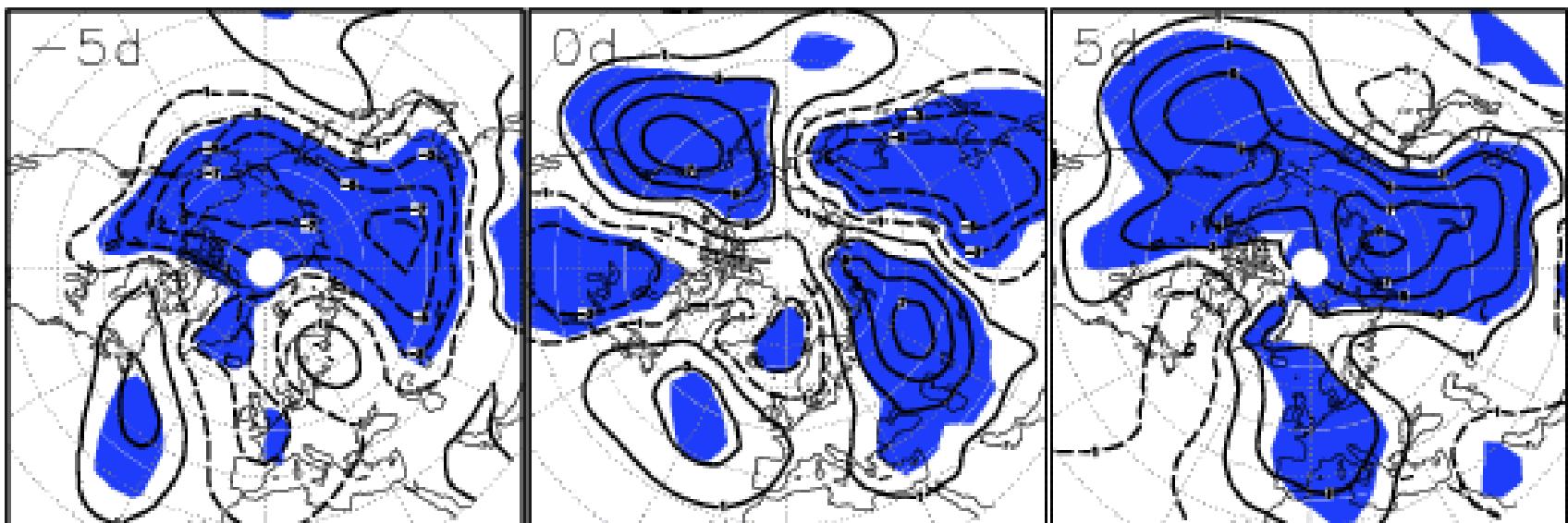
*Composites of surface pressure anomaly keyed on the total Equatorial Torque (LMDz) and on the Equatorial Mountain Torque (NCEP)*

**Issue : does the same improvement occurs for the south-American cold surges?**

# Dynamical impact of mountains on atmospheric flows

## f) Planetary scales dynamics

Interaction between a  $s=2-3$  planetary wave in surface pressure and the large scale mountains. See the global deceleration within 10 days associated with the negative mountain torque produced by the wave.



# Dynamical impact of mountains on atmospheric flows

## g) Summary of issues

Theory (and or mesoscale modelling): trapped lee waves and PBL, interaction between valley weather and the large scale weather ?

SSO parameterization : Directionnal effects, trapped waves, stochastic formulation

Impacts :

On local weather events like cold surges and (most of all) precipitations !

On the southern hemisphere stratosphere, rôle of the isolated islands?

In a changing climate

Analysis of the influence of mountains in the on-going CMIP simulations ? In order to list the errors to be corrected ?

Observations (?)

Mesoscale modelling approach (?)